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## Some results on the Baire Rado Conjecture

Baire Rado's Conjecture ( $RC^b$  in short, introduced by Todorćević as a weakening of the Rado's Conjecture) asserts that any non-trivial Baire tree of height  $\omega_1$  has a nonspecial subtree of size  $\leq \aleph_1$ . It is incompatible with MA. This work is motivated by the question "which fragment of forcing axioms is compatible with  $RC^b$ ". A poset is Baire Indestructibly Proper (BIP) if it remains proper in any forcing extension by a Baire tree. We will show  $RC^b$  is compatible with  $MA_{\omega_1}(BIP)$  and as a consequence  $RC^b$  does not imply  $RC$ . If time permits we will talk about the interaction of  $RC^b$  with other combinatorial principles like simultaneous stationary reflection, versions of weak squares and polarized partition relations.

- [1] Jing Zhang, Rado's Conjecture and its Baire Version. preprint, <https://arxiv.org/abs/1712.02455>.